Presentation at Research Group DALE: Differential Accumulated Local Effects for efficient and accurate global explanations

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March 2023

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• Vasilis Gkolemis:

- Research Assistant at ATHENA Research Center (ATHENA RC)
- First-year PhD at Harokopio University of Athens (HUA)
- Main focus: Explainability under uncertainty
- Supervisors:
 - Christos Diou (HUA) \rightarrow Generalization, Few(Zero)-shot learning
 - ► Eirini Ntoutsi (UniBw-M) → Explainability, Fairness
 - Theodore Dalamagas (ATHENA) \rightarrow Databases, data semantics
- Paper I will present
 - DALE: Differential Accumulated Local Effects for efficient and accurate global explanations
 - ► Accepted at Asian Conference Machine Learning (ACML) 2022

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- Why did the model make a specific decision? local XAI
- What could we change so that the model will make a different decision? counterfactual
- Can we summarize the model's behavior? global XAI
- If models are knowledge extractors, what have they learned? global XAI

Feature Effect: global, model-agnostic, outputs a 1D plot

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Consider the following mapping $x \rightarrow y$



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Process unknown \rightarrow we only have samples



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Our goal is to model the process using the available samples (regression)

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Linear model \rightarrow Underfiting!

$$y = w_1 \cdot x + w_0$$



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 2^{nd} degree polynomial \rightarrow Decent Fit!

$$y = w_2 \cdot x^2 + w_1 \cdot x + w_0$$



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 3^{rd} degree polynomial \rightarrow Good Fit!

$$y = w_3 \cdot x^3 + w_2 \cdot x^2 + w_1 \cdot x + w_0$$



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 9^{th} degree polynomial \rightarrow Overfitting!

$$y = \sum_{i=0}^{9} w_i \cdot x^i$$



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- Model behavior is explained by the shape of the function
- Overfitting, Underfitting are easily diagnosed
- If the input has multiple dimensions D?
 - We often have tens or hundreds of features
 - Images and signals: Several thousands of input dimensions
- Example: Risk Factors for Cervical Cancer Dataset
 - input: 15 features (smoker, years of hormonal contraceptives, age)
 - output: predict whether a woman will get cervical cancer

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Feature Effect

 $y = f(x_s) \rightarrow \text{plot showing the effect of } x_s \text{ on the output } y$



Figure: Image taken from Interpretable ML book (Molnar, 2022)

Feature Effect is simple	and intuitive.	ㅁ › 《畵 › 《콜 › 《콜 ›	≣ <i>•</i>)९.२
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- $x_s \rightarrow$ feature of interest, $x_c \rightarrow$ other features
- Isolating the effect of x_s is a difficult task:
 - features are correlated
 - f has learned complex interactions
- Three well-known methods:
 - Partial Dependence Plots (PDP)
 - M-Plots
 - Accumulated Local Effects (ALE)

Partial Dependence Plots (PDP)

• Proposed by J. Friedman on 2001¹ and is the marginal effect of a feature to the model output:

$$f_s(x_s) = \mathbb{E}_{\mathbf{x}_c} \left[f(x_s, \mathbf{x}_c) \right] = \int f(x_s, \mathbf{x}_c) p(\mathbf{x}_c) d\mathbf{x}_c$$

where:

- *x_s* is the feature whose effect we wish to compute
- *x_c* are the rest of the features
- Approximation:

$$\hat{f}_s(x_s) = \frac{1}{n} \sum_{i=1}^n f(x_s, \mathbf{x}_c^{(i)})$$

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Issues with PDPs



Figure: C. Molnar, IML book

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- Correlated features
 - To compute the effect of x_{age} = 20 on the output (cancer probability) it will integrate over all x_{years_contraceptives} values, e.g., [0, 50]
 - ▶ f can have weird behavior when x_{age} = 20, x_{years_contraceptives} = 20 (out of distribution)
 - As a result, we have a wrong estimation of the feature effect

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MPlots

• We use the value of x_s as a condition, so we integrate over $\mathbf{x}_c | x_s$

$$f(x_s) = \mathbb{E}_{\mathbf{x}_c | x_s}[f(x_s, \mathbf{x}_c)] = \int f(x_s, \mathbf{x}_c) p(\mathbf{x}_c | x_s) d\mathbf{x}_c$$

where:

- ► *x_s* is the feature whose effect we wish to compute
- *x_c* the rest of the features
- Approximation:

$$f_{s}(x_{s}) = \frac{1}{n} \sum_{i: x_{s}^{(i)} \approx x_{s}} f(x_{s}, \mathbf{x}_{c}^{(i)})$$

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MPlots

In the previous example



Figure: C. Molnar, IML book

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Image: A (1)

- Aggregated effect symptom \rightarrow the calculated effects result from the combination of all (correlated) features
- Real effect:
 - ► x_{age} = 50 → 10
 - $x_{\text{years_contraceptives}} = 20 \rightarrow 10$
 - aggregated effect close to 20

• Because $x_{age}, x_{years_contraceptives}$ are correlated, MPlot may assign:

- $x_{\text{age}} = 50 \rightarrow 17 \approx \text{aggregated effect}$
- $x_{\text{years_contraceptives}} = 20 \rightarrow 17 \approx \text{aggregated effect}$

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• Resolves problems that result from the feature correlation by computing differences over a (small) window

$$f(x_{s}) = \int_{x_{min}}^{x_{s}} \mathbb{E}_{\substack{\mathbf{x}_{c} \mid Z \\ realistic}} [\frac{\partial f}{\partial x_{s}}(z, \mathbf{x}_{c})] \partial z$$

²D. Apley and J. Zhu. "Visualizing the effects of predictor variables in black box supervised learning models." Journal of the Royal Statistical Society: Series B (Statistical Methodology) 82.4 (2020): 1059-1086.

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ALE approximation

ALE definition: $f(x_s) = \int_{x_{s,min}}^{x_s} \mathbb{E}_{\mathbf{x_c}|z}[\frac{\partial f}{\partial x_s}(z, \mathbf{x_c})]\partial z$ ALE approximation: $f(x_s) = \sum_{k}^{k_x} \frac{1}{|\mathcal{S}_k|} \sum_{i: \mathbf{x}^i \in \mathcal{S}_k} \underbrace{[f(z_k, \mathbf{x}_c^i) - f(z_{k-1}, \mathbf{x}_c^i)]}_{\text{point effect}}$ bin effect 1.00 N1(1) N1(2) N1(3) N1(4) N1(5) 0.75 N 0.25 0.00 -Z2.1 Z6.1 x1

Figure: Image taken from Interpretable ML book (Molnar, 2022)

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ALE approximation - weaknesses

$$f(x_s) = \sum_{k}^{k_x} \underbrace{\frac{1}{|\mathcal{S}_k|} \sum_{i: \mathbf{x}^i \in \mathcal{S}_k} \underbrace{[f(z_k, \mathbf{x}_c^i) - f(z_{k-1}, \mathbf{x}_c^i)]}_{\text{point effect}}}_{\text{bin effect}}$$

Point Effect ⇒ evaluation at bin limits

- 2 evaluations of f per point \rightarrow slow
- change bin limits, pay again 2 * N evaluations of $f \rightarrow$ restrictive
- ▶ broad bins may create out of distribution (OOD) samples → not-robust in wide bins

ALE approximation has some weaknesses

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- $\bullet~\mathsf{PDP} \to \mathsf{problems}$ with correlated features \to Unrealistic instances
- $\bullet~$ MPlot \rightarrow problems with correlated features \rightarrow Aggregated effects
- ALE \rightarrow resolves both issues! But:
- ALE approximation (estimation of ALE from the training set)
 - slow when there are many features
 - unrealistic instances when bins become bigger
- Differential ALE (DALE)!

Our proposal: Differential ALE



Point Effect ⇒ evaluation on instances

- Fast \rightarrow use of auto-differentiation, all derivatives in a single pass
- \blacktriangleright Versatile \rightarrow point effects computed once, change bins without cost
- Secure \rightarrow does not create artificial instances

For differentiable models, DALE resolves ALE weaknesses

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DALE is faster and versatile - theory



- Faster
 - gradients wrt all features $\nabla_{\mathbf{x}} f(\mathbf{x}^{i})$ in a single pass
 - auto-differentiation must be available (deep learning)
- Versatile
 - Change bin limits, with near zero computational cost

DALE is faster and allows redefining bin-limits

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DALE is faster and versatile - Experiments



Figure: Light setup; small dataset ($N = 10^2$ instances), light f. Heavy setup; big dataset ($N = 10^5$ instances), heavy f

DALE considerably accelerates the estimation

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DALE uses on-distribution samples - Theory



- point effect independent of bin limits
 - $\frac{\partial f}{\partial x_s}(x_s^i, x_c^i)$ computed on real instances $x^i = (x_s^i, x_c^i)$
- bin limits affect only the resolution of the plot
 - \blacktriangleright wide bins \rightarrow low resolution plot, bin estimation from more points
 - \blacktriangleright narrow bins \rightarrow high resolution plot, bin estimation from less points

DALE enables wide bins without creating out of distribution instances

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DALE uses on-distribution samples - Experiments

$$f(x_1, x_2, x_3) = x_1 x_2 + x_1 x_3 \pm g(x)$$
$$x_1 \in [0, 10], x_2 \sim x_1 + \epsilon, x_3 \sim \mathcal{N}(0, \sigma^2)$$
$$f_{ALE}(x_1) = \frac{x_1^2}{2}$$

- point effects affected by (x₁x₃) (σ is large)
- bin estimation is noisy (samples are few)



Intuition: we need wider bins (more samples per bin)

DALE vs ALE - 40 Bins



- \bullet DALE: on-distribution, noisy bin effect \rightarrow poor estimation
- ALE: on-distribution, noisy bin effect \rightarrow poor estimation

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DALE vs ALE - 40 Bins



- \bullet DALE: on-distribution, noisy bin effect \rightarrow poor estimation
- ALE: on-distribution, noisy bin effect \rightarrow poor estimation

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DALE vs ALE - 20 Bins



- \bullet DALE: on-distribution, noisy bin effect \rightarrow poor estimation
- ALE: on-distribution, noisy bin effect \rightarrow poor estimation

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DALE vs ALE - 20 Bins



- \bullet DALE: on-distribution, noisy bin effect \rightarrow poor estimation
- ALE: on-distribution, noisy bin effect \rightarrow poor estimation

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DALE vs ALE - 10 Bins



- DALE: on-distribution, noisy bin effect \rightarrow poor estimation
- ALE: starts being OOD, noisy bin effect \rightarrow poor estimation.

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DALE vs ALE - 10 Bins



- \bullet DALE: on-distribution, noisy bin effect \rightarrow poor estimation
- ALE: starts being OOD, noisy bin effect \rightarrow poor estimation

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Image: A math

DALE vs ALE - 5 Bins



DALE: on-distribution, robust bin effect → good estimation
ALE: completely OOD, robust bin effect → poor estimation_

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DALE vs ALE - 5 Bins



- DALE: on-distribution, robust bin effect \rightarrow good estimation
- ALE: completely OOD, robust bin effect \rightarrow poor estimation

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DALE vs ALE - 3 Bins



DALE: on-distribution, robust bin effect → good estimation
ALE: completely OOD, robust bin effect → poor estimation_

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DALE vs ALE - 3 Bins



- DALE: on-distribution, robust bin effect \rightarrow good estimation
- ALE: completely OOD, robust bin effect \rightarrow poor estimation

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Future Ideas (1)

PDPs use ICE plots, for exhibiting heterogeneity



Figure: PDP plot, taken from Goldstein et. al

Interpretation? Maybe $y \perp x_2$

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Future Ideas (2)

PDPs use ICE plots, for exhibiting heterogeneity



Figure: PDP-ICE plot, taken from Goldstein et. al

Interpretation now? Maybe $y \approx \pm 6x_2$ depending on a condition

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Future Ideas (3)

• Could ALE plots do the same?

• Variance inside each bin?



Figure: (Left) PDP-ICE (Right) ALE with heterogeneity

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Future Ideas (4) - Regional Effect plots

 $\bullet~$ Heterogeneity \rightarrow subspaces with homogeneous effects



Figure: REPID: Regional Effect plots, taken from Herbinger et. al

Same idea on ALE?	< 1	미 › 《圊 › 《콜 › 《콜 › 콜	୬୯୯
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Thank you

• Questions?

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Fanaee-T, Hadi and Joao Gama (2013). "Event labeling combining ensemble detectors and background knowledge". In: Progress in Artificial Intelligence, pp. 1–15. ISSN: 2192-6352. DOI: 10.1007/s13748-013-0040-3. URL: [WebLink].
Molnar, Christoph (2022). Interpretable Machine Learning. A Guide for Making Black Box Models Explainable. 2nd ed. URL: https://christophm.github.io/interpretable-ml-book.

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